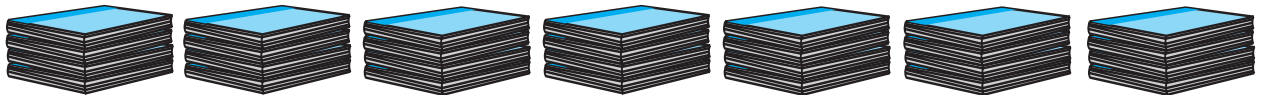


**Let's recall.**

Each of 7 children was given 4 books.

Total notebooks = $4 + 4 + 4 + 4 + 4 + 4 + 4 = 28$ notebooks



Here, addition is the operation that is carried out repeatedly.

Addition of the same number again and again can be shown as a multiplication.

Total notebooks = $4 + 4 + 4 + 4 + 4 + 4 + 4 = 4 \times 7 = 28$

**Let's learn.****Base and Index**

Let us see how the multiplication of a number by itself several times is expressed in short.

$2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2$: Here, 2 is multiplied by itself 8 times.

This is written as 2^8 in short. This is the index form of the multiplication.

Here, 2 is called the **base** and 8, the **index** or the **exponent**.

8	←	Index
2	←	Base

Example $5 \times 5 \times 5 \times 5 = 5^4$ Here 5^4 is in the index form.

In the number 5^4 , 5 is the base and 4 is the index.

This is read as '5 raised to the power 4' or '5 raised to 4', or 'the 4th power of 5'.

Generally, if a is any number, $a \times a \times a \times \dots \times a$ (m times) = a^m

Read a^m as 'a raised to the power m' or 'the mth power of a'.

Here m is a natural number.

$\therefore 5^4 = 5 \times 5 \times 5 \times 5 = 625$. Or, the value of the number $5^4 = 625$.

Similarly, $\left[\frac{-2}{3}\right]^3 = \frac{-2}{3} \times \frac{-2}{3} \times \frac{-2}{3} = \frac{-8}{27}$ means that the value of $\left[\frac{-2}{3}\right]^3$ is $\frac{-8}{27}$.

Note that $7^1 = 7$, $10^1 = 10$. **The first power of any number is that number itself.** If the power or index of a number is 1, the convention is not to write it.

Thus $5^1 = 5$, $a^1 = a$.

Practice Set 26

1. Complete the table below.

Sr. No.	Indices (Numbers in index form)	Base	Index	Multiplication form	Value
(i)	3^4	3	4	$3 \times 3 \times 3 \times 3$	81
(ii)	16^3				
(iii)		(-8)	2		
(iv)				$\frac{3}{7} \times \frac{3}{7} \times \frac{3}{7} \times \frac{3}{7}$	$\frac{81}{2401}$
(v)	$(-13)^4$				

2. Find the value.

- (i) 2^{10} (ii) 5^3 (iii) $(-7)^4$ (iv) $(-6)^3$ (v) 9^3
 (vi) 8^1 (vii) $\left(\frac{4}{5}\right)^3$ (viii) $\left(-\frac{1}{2}\right)^4$

Square and Cube

$$3^2 = 3 \times 3$$

3^2 is read as '3 raised to 2'

or 3 'squared' or 'the square of 3'

$$5^3 = 5 \times 5 \times 5$$

5^3 is read as '5 raised to 3'

or '5 cubed' or 'the cube of 5'.

Remember :

**The second power of any number is the square of that number.
 The third power of any number is the cube of that number.**



Let's learn.

Multiplication of Indices with the Same Base.

Example $2^4 \times 2^3$

$$= 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2$$

$$= 2^7$$

Therefore, $2^4 \times 2^3 = 2^{4+3} = 2^7$

Example $(-3)^2 \times (-3)^3$

$$= (-3) \times (-3) \times (-3) \times (-3) \times (-3)$$

$$= (-3)^5$$

Therefore, $(-3)^2 \times (-3)^3 = (-3)^{2+3} = (-3)^5$

Example $\left(\frac{-2}{5}\right)^2 \times \left(\frac{-2}{5}\right)^3 = \left(\frac{-2}{5}\right) \times \left(\frac{-2}{5}\right) \times \left(\frac{-2}{5}\right) \times \left(\frac{-2}{5}\right) \times \left(\frac{-2}{5}\right) = \left(\frac{-2}{5}\right)^5$

Therefore, $\left(\frac{-2}{5}\right)^2 \times \left(\frac{-2}{5}\right)^3 = \left(\frac{-2}{5}\right)^{2+3} = \left(\frac{-2}{5}\right)^5$

**Now I know!**

If a is a rational number and m and n are positive integers, then $a^m \times a^n = a^{m+n}$

Practice Set 27

(1) Simplify.

(i) $7^4 \times 7^2$

(ii) $(-11)^5 \times (-11)^2$

(iii) $\left(\frac{6}{7}\right)^3 \times \left(\frac{6}{7}\right)^5$

(iv) $\left(-\frac{3}{2}\right)^5 \times \left(-\frac{3}{2}\right)^3$

(v) $a^{16} \times a^7$

(vi) $\left(\frac{P}{5}\right)^3 \times \left(\frac{P}{5}\right)^7$

**Let's learn.****Division of Indices with the Same Base****Example** $6^4 \div 6^2 = ?$

$$\frac{6^4}{6^2} = \frac{6 \times 6 \times 6 \times 6}{6 \times 6}$$

$$= 6 \times 6$$

$$= 6^2$$

$$\therefore 6^4 \div 6^2 = 6^{4-2} = 6^2$$

Example $(-2)^5 \div (-2)^3 = ?$

$$\frac{(-2)^5}{(-2)^3} = \frac{(-2) \times (-2) \times (-2) \times (-2) \times (-2)}{(-2) \times (-2) \times (-2)}$$

$$= (-2)^2$$

$$\therefore (-2)^5 \div (-2)^3 = (-2)^2$$

**Now I know!**

If a is a non-zero rational number, m and n are positive integers and $m > n$, then $\frac{a^m}{a^n} = a^{m-n}$

The meaning of a^0 If $a \neq 0$

Then $\frac{a^m}{a^m} = 1$

Also, $\frac{a^m}{a^m} = a^{m-m} = a^0$

$$\therefore \boxed{a^0 = 1}$$

The meaning of a^{-m}

$a^{-m} = a^{-m} \times 1$

$= a^{-m} \times \frac{a^m}{a^m}$

$= \frac{a^{-m+m}}{a^m}$

$= \frac{a^0}{a^m} = \frac{1}{a^m}$

$$\boxed{a^{-m} = \frac{1}{a^m}}$$

$a^{-m} = \frac{1}{a^m} \therefore a^{-1} = \frac{1}{a}$

$a \times \frac{1}{a} = 1, \therefore a \times a^{-1} = 1$

 $\therefore a^{-1}$ is the multiplicative inverse of a .

Thus, the multiplicative inverse

of $\frac{5}{3}$ is $\frac{3}{5}$.

$$\therefore \boxed{\left(\frac{5}{3}\right)^{-1} = \frac{3}{5}}$$

Example Let us consider $\left(\frac{4}{7}\right)^{-3} \cdot \left(\frac{4}{7}\right)^{-3} = \frac{1}{\frac{4}{7} \times \frac{4}{7} \times \frac{4}{7}} = \frac{1}{\frac{64}{343}} = \frac{343}{64} = \left(\frac{7}{4}\right)^3$



Now I know!

Hence, we get the rule that if $a \neq 0$, $b \neq 0$ and m is a positive integer,

$$\text{then } \left(\frac{a}{b}\right)^{-m} = \left(\frac{b}{a}\right)^m$$

Let us see what rule we get by observing the following examples :

Example $(3)^4 \div (3)^6$

$$\begin{aligned} &= \frac{3^4}{3^6} \\ &= \frac{3 \times 3 \times 3 \times 3}{3 \times 3 \times 3 \times 3 \times 3 \times 3} = \frac{1}{3^2} \\ 3^4 \div 3^6 &= 3^{4-6} = 3^{-2} \end{aligned}$$

Example $\left(\frac{3}{5}\right)^2 \div \left(\frac{3}{5}\right)^5$

$$\begin{aligned} &= \frac{\frac{3}{5} \times \frac{3}{5}}{\frac{3}{5} \times \frac{3}{5} \times \frac{3}{5} \times \frac{3}{5} \times \frac{3}{5}} = \frac{1}{\frac{3}{5} \times \frac{3}{5} \times \frac{3}{5}} = \frac{1}{\left(\frac{3}{5}\right)^3} \\ \therefore \left(\frac{3}{5}\right)^2 \div \left(\frac{3}{5}\right)^5 &= \left(\frac{3}{5}\right)^{2-5} = \left(\frac{3}{5}\right)^{-3} \end{aligned}$$



Now I know!

If a is a rational number, $a \neq 0$ and m and n are positive integers, then $\frac{a^m}{a^n} = a^{m-n}$



Let's learn.

Observe what happens if the base is (-1) and the index is a whole number.

$$(-1)^6 = \underline{(-1)} \times \underline{(-1)} \times \underline{(-1)} \times \underline{(-1)} \times \underline{(-1)} \times \underline{(-1)} = 1 \times 1 \times 1 = 1$$

$$(-1)^5 = \underline{(-1)} \times \underline{(-1)} \times \underline{(-1)} \times \underline{(-1)} \times \underline{(-1)} = 1 \times 1 \times (-1) = -1$$

If m is an even number then $(-1)^m = 1$, and if m is an odd number, then $(-1)^m = -1$

Practice Set 28

1. Simplify.

(i) $a^6 \div a^4$

(ii) $m^5 \div m^8$

(iii) $p^3 \div p^{13}$

(iv) $x^{10} \div x^{10}$

2. Find the value.

(i) $(-7)^{12} \div (-7)^{12}$

(ii) $7^5 \div 7^3$

(iii) $\left(\frac{4}{5}\right)^3 \div \left(\frac{4}{5}\right)^2$

(iv) $4^7 \div 4^5$



Let's learn.

The Index of the Product or Quotient of Two Numbers

Let us observe the following examples to see what rule we get.

Example $(2 \times 3)^4$

$$= (2 \times 3) \times (2 \times 3) \times (2 \times 3) \times (2 \times 3)$$

$$= 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 3 = 2^4 \times 3^4$$

Example $\left(\frac{4}{5}\right)^3$

$$= \frac{4}{5} \times \frac{4}{5} \times \frac{4}{5}$$

$$= \frac{4 \times 4 \times 4}{5 \times 5 \times 5} = \frac{4^3}{5^3}$$



Now I know!

If a and b are non-zero rational numbers and m is an integer, then

$$(1) (a \times b)^m = a^m \times b^m \quad (2) \left(\frac{a}{b}\right)^m = \frac{a^m}{b^m}$$

$(a^m)^n$, that is, the Power of a Number in Index Form

Example $(5^2)^3$

$$= 5^2 \times 5^2 \times 5^2$$

$$= 5^{2+2+2}$$

$$= 5^{2 \times 3}$$

$$= 5^6$$

Example $(7^{-2})^{-5} = \frac{1}{(7^{-2})^5}$

$$= \frac{1}{7^{-2} \times 7^{-2} \times 7^{-2} \times 7^{-2} \times 7^{-2}}$$

$$= \frac{1}{7^{(-2) \times 5}}$$

$$= \frac{1}{7^{-10}} = 7^{10}$$

$$a^{-m} = \frac{1}{a^m}$$

Example $\left(\left(\frac{2}{5}\right)^{-2}\right)^3$

$$= \left(\frac{2}{5}\right)^{-2} \times \left(\frac{2}{5}\right)^{-2} \times \left(\frac{2}{5}\right)^{-2} = \left(\frac{2}{5}\right)^{(-2)+(-2)+(-2)} = \left(\frac{2}{5}\right)^{-6}$$

$$(a^m)^n = a^m \times a^m \times a^m \times \dots \times a^m \text{ } n \text{ times} = a^{m+m+m \dots m} \text{ } n \text{ times} = a^{m \times n}$$

From the above examples, we get the following rule.



Now I know!

If a is a non-zero rational number and m and n are integers, then $(a^m)^n = a^{m \times n} = a^{mn}$

**Let's recall.****Finding the square root of a perfect square**

When a number is multiplied by itself the product obtained is the square of the number.

Example $6 \times 6 = 6^2 = 36$

$6^2 = 36$ is read as 'The square of 6 is 36.'

Example $(-5) \times (-5) = (-5)^2 = 25$

$(-5)^2 = 25$ is read as 'The square of (-5) is 25.'

**Let's learn.***** Finding the square root of a given number**

Example $3 \times 3 = 3^2 = 9$ Here, the square of 3 is 9.

Or, we can say that the square root of 9 is 3.

The symbol $\sqrt{\quad}$ is used for 'square root'.

$\sqrt{9}$ means the square root of 9. $\therefore \sqrt{9} = 3$

Example $7 \times 7 = 7^2 = 49$ $\therefore \sqrt{49} = 7$

Example $8 \times 8 = 8^2 = 64$. Hence $\sqrt{64} = 8$

$(-8) \times (-8) = (-8)^2 = 64$. Hence, $\sqrt{64} = -8$.

Thus, if x is a positive number, it has two square roots.

Of these, the negative square root is shown as $-\sqrt{x}$ and the positive one as \sqrt{x} .

Example Find the square root of 81.

$81 = 9 \times 9 = -9 \times -9$ $\therefore \sqrt{81} = 9$ and $-\sqrt{81} = -9$

Mostly, we consider the positive square root.

*** Finding the square root by the factors method**

Example Find the square root of 144.

Find the prime factors of the given number and put them in pairs of equal numbers.

$$\begin{aligned} 144 &= 2 \times 72 \\ &= 2 \times 2 \times 36 \\ &= 2 \times 2 \times 2 \times 18 \\ &= \underline{2 \times 2} \times \underline{2 \times 2} \times \underline{3 \times 3} \end{aligned}$$

Form pairs of equal factors from the prime factors obtained.

Take one factor from each pair and multiply.

$\sqrt{144} = 2 \times 2 \times 3 = 12$ $\therefore \sqrt{144} = 12$

2	144
2	72
2	36
2	18
3	9
3	3
	1

Example Find the square root of 324.

Find the prime factors of the given number and put them in pairs of equal factors.

$$\begin{aligned} 324 &= 2 \times 162 \\ &= 2 \times 2 \times 81 \\ &= 2 \times 2 \times 3 \times 27 \\ &= 2 \times 2 \times 3 \times 3 \times 9 \\ &= \underline{2 \times 2} \times \underline{3 \times 3} \times \underline{3 \times 3} \end{aligned}$$

2	324
2	162
3	81
3	27
3	9
3	3
	1

To find the square root, take one number from each pair and multiply.

$$\sqrt{324} = 2 \times 3 \times 3 = 18$$

$$\therefore \sqrt{324} = 18$$

Practice Set 30

- ⊙ Find the square root. (i) 625 (ii) 1225 (iii) 289 (iv) 4096 (v) 1089

* Something more (Square root by the division method)

Find the square root of :

(1) 9801

	99
9	$\overline{9801}$
+ 9	$\overline{81}$
189	1701
+ 9	$\overline{1701}$
198	0000

$$\sqrt{9801} = 99$$

(2) 19321

	139
1	$\overline{19321}$
+ 1	$\overline{1}$
23	093
+ 3	$\overline{69}$
269	2421
+ 9	$\overline{2421}$
278	0000

(3) 141.61

	11.9
1	$\overline{141.61}$
+ 1	$\overline{1}$
21	041
+ 1	$\overline{21}$
229	2061
+ 9	$\overline{2061}$
238	0000

This method can be used to find the square root of numbers which have many prime factors and are, therefore, difficult to factorise.

Now let us take $\sqrt{137}$ to see one more use.

	11.7
1	$\overline{137.00}$
+ 1	$\overline{-1}$
21	037
+ 1	$\overline{-21}$
227	1600
+ 7	$\overline{1589}$
234	11

$$\sqrt{137} > 11.7$$

$$\text{But } (11.8)^2 = 139.24$$

$$\therefore 11.7 < \sqrt{137} < 11.8$$

Thus, we can find the approximate value of $\sqrt{137}$. This method can be used to find the approximate square root of a number whose square root is not a whole number.

